

## **Analysis of Spectrum Sensing By Using Energy Detection Technique in Cognitive Radio**

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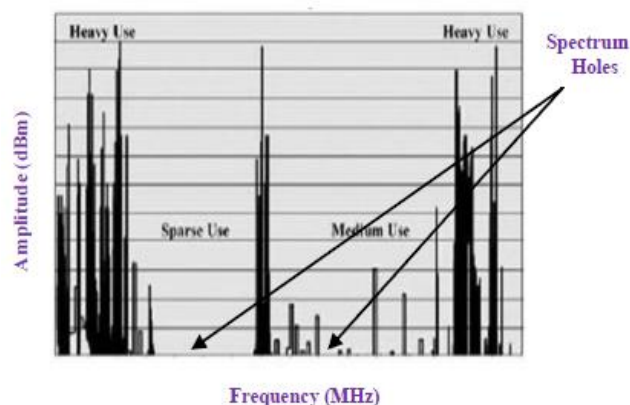
**Abstract:** In wireless technologies the importance of spectrum is rapidly increases hence traffic of spectrum is also increases day by day. However, it seems that the current technologies do not utilize the licensed spectrum bands efficiently (6). So, energy detection in cognitive radio is proposed to improve the spectrum utilization. Cognitive Radios are the secondary users of the allocated spectrum bands for the primary users. In the cognitive radio system, the signal detection technique is required for spectrum sensing in order to sense the occupied and vacant bands. The challenge of spectrum sensing is the detection of poor signals in the presence of noise and interference (7).

In this paper, have evaluated the performance of energy detection system under the real noise at -10dB, -15dB & -20dB SNR using energy detection. In general Energy detector is the one of the method used in spectrum sensing due to its simplicity; it requires no need of synchronization and knowledge of transmission information through the transmitter.

**Keywords:** Cognitive Radio, Spectrum Utilization, Hypotheses, Pd, Pfa, AWGN, White Spaces

### **I. INTRODUCTION**

In a wireless communication system the electromagnetic spectrums becoming crowded day by day due to the increment of wireless applications. In which the cognitive radio plays a very important role for spectrum sensing. In which it is observed that the available spectrum is not utilized properly at that time and particular geographic location. To overcome this problem the cognitive radio technology is proposed to sense unused bands. Cognitive Radio is to provide effective communication and utilization of spectrum bands for users. Cognitive Radio having the ability to determine the presence of the licensed user, and also detects which portion of spectrum is available, in other words, to detect the white spaces that means empty bands, which is known as spectrum sensing. The energy based detector is the easier method for sensing primary users in the environment. The energy detector is very convenient technique and also computationally efficient with analog and digital signals. It gives the poor performance when noise variance is unknown to the sensing node. Therefore, it is difficult to distinguish between the radio signal and noise signal at very low SNR. So that it is necessary to know the information of the noise power which can be used to improve the efficiency of the energy detector [6]



**Fig.1. Utilization of the spectrum<sup>[1]</sup>**

Cognitive Radio is a technology used for detection of vacant bands and utilized the same for improving the performance of spectrum sensing without affecting on Primary Users (PU) [2].

## II. ENERGY DETECTOR MODEL

Energy detection is a simple technique to detect the primary signal based on energy of received signal and the advantageous as no need of prerequisites of primary user signals to detect the presence or absence of signal in the spectrum band. The approaches used in the energy detection are based on the Bayes Test & Neyman-Pearson (NP) Test. The NP is most preferable approach in Energy detection. Because, it increases the probability of detection (Pd) for a given probability of false alarm (Pfa). In this paper, the QPSK signal is transmitted through the Rayleigh fading environment with an additive white Gaussian noise (AWGN) channel

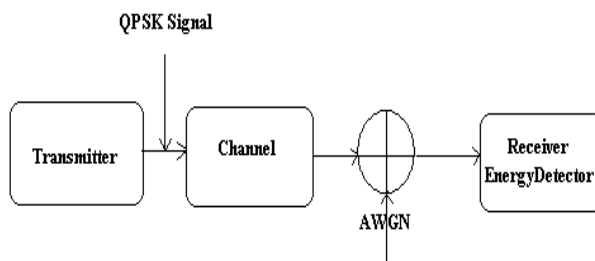


Fig.2 Block diagram of Trans-receiver

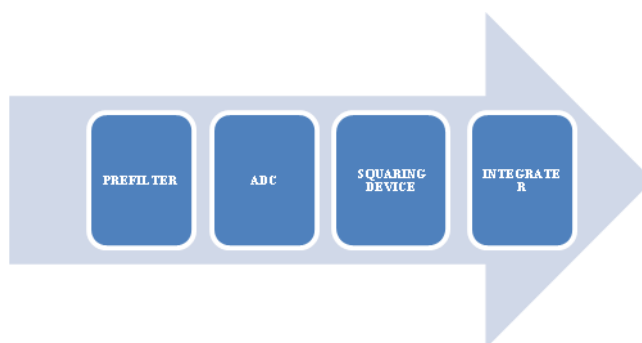


Fig.3 Block diagram of the energy detector

## III. STATISTICAL ANALYSIS

Within certain time, energy detector measures the energy of the signal and compares it with the threshold. Energy detection is commonly modelled based on hypothesis testing problem and then performance is have evaluated by probability of false alarm and probability of detection. In this paper the problem is analyzed by mathematically and then evaluated the threshold. As shown in fig.3 the prefilter is used as a band pass filter of bandwidth  $W$ . The output of band pass filter passes through the squaring device and then integrated over a predefined sensing time  $T$ . The integrator output is compared with a threshold to take a decision between two hypotheses. By using Nyquist sampling theory, each sample of the received signal is expressed as,

$$r_i = r \frac{i}{2W} \quad (i=1, 2, \dots, +\infty) \quad (1)$$

Where,  $W$  is the bandwidth  $T_s$  is the symbol duration of the signal [3]. Here the energy per sample is defined as  $E_s$ ,

$$P_s = E_s / T_s = E. \quad (2)$$

$R$  is a symbol rate of the system. Therefore, energy of observed transmitted signal per sample is,

$$\frac{P_s T}{2WT} = (3)$$

Thus, the energy per sample of noise signal at the pre filter output is,

$$\frac{2N_0WT}{2WT} = \frac{2N_0W}{2W} = N_0 \quad (4)$$

$N_o$  represents the two sided noise power density. If there is only noise signal present, the energy of receiving signal is expressed as,

$$V = \int_0^T n^2(t) dt = \frac{1}{2W} \sum_{i=1}^{2TW} n_i^2 \quad (5)$$

The Gaussian random variable with zero mean and variance as follows respectively,

$$n_i = n(i/2W) \quad (6)$$

$$\sigma_i^2 = 2WN_o \quad (7)$$

By using the definition of chi-square distribution the chi-square PDF arises as the PDF of  $x$  where <sup>[4]</sup>

$$x = \sum_{i=1}^N n_i^2 \quad (8)$$

From the above equation we find the variance of  $n_i$  must be normalized to 1.

$$b_i = \frac{n_i}{\sqrt{2WN_o}} \quad (9)$$

Here  $V'$  is monotonic with  $V$  to represent statistic test as

$$V' = \frac{1}{N_o} V = \frac{1}{N_o} \int_0^T n^2(t) dt$$

$$V' = \frac{1}{N_o} \int_0^T n^2(t) dt = \frac{1}{2WN_o} \sum_{i=1}^{2TW} n_i^2 = \sum_{i=1}^{2TW} b_i^2 \quad (10)$$

The simple form is,

$$V' = \sum_{i=1}^{2TW} b_i^2 \quad (11)$$

After normalization we obtain the statistic test as,

$$V' = \frac{1}{N_o} V = \frac{1}{N_o} \int_0^T s^2(t) dt = \sum_{i=1}^{2TW} \beta_i^2 \quad (12)$$

Where,

$$\beta_i = \frac{\alpha_i}{\sqrt{2WN_o}}$$

So energy of received signal in interval (0,T) is

$$V = \int_0^T r^2(t) dt = \frac{1}{2W} \sum_{i=1}^{2TW} (\alpha_i + b_i)^2 \quad (13)$$

And statistic test is given by normalized value

$$V' = \int_0^T r^2(t)dt = \frac{1}{2TW} \sum_{i=1}^{2TW} (\beta_i + b_i)^2 \quad (14)$$

Where  $\beta_i$  is  $V'$  the normalized primary signal and  $b_i$  is the normalized noise signal

Therefore when signal is present the,  $V'$  considered the chi square distribution with  $N$  degree of freedom and noncentral parameter  $\gamma$ .

$$\gamma = \sum_{i=1}^{2TW} \beta_i^2 = \frac{1}{N_0} \int_0^T S^2(t)dt = \frac{E_T}{N_0} \quad (15)$$

Where  $E_T$  represents the signal energy in time interval  $T$ . The noncentral parameter  $\gamma$  is defined as the SNR

From the chi-square distribution, we may represent the statistic test as

$$V' = \begin{cases} x_N^2 & H_0 \\ x_N^2(\gamma) & H_1 \end{cases} \quad (16)$$

Where,

$N=2TW$  is the number of degrees of freedom,

$x_N^2$  Represents the chi-square distribution and

$x_N^2(\gamma)$  Represents non central chi-square distribution.

### THRESHOLD DERIVATION

For energy detection the  $P_{fa}$  is predefined and only depends on the noise variance and  $N$ , therefore threshold can be set without prior knowledge of primary users. So we can select the threshold to obtain a fixed  $P_{fa}$  and then calculate the probability of detection  $P_d$ .

Threshold can be derived by PDF of the,  $V'$  under two hypotheses [4]

$$H_0 : f_{V'}\left(\frac{x}{H_0}\right) = \frac{1}{2TW} x^{\frac{N}{2}-1} \exp\left(-\frac{1}{2}x\right) \quad (17)$$

$$H_1 : f_{V'}\left(\frac{x}{H_1}\right) = \frac{1}{2} \left(\frac{x}{\gamma}\right)^{\frac{N-2}{2}} \exp\left(-\frac{1}{2}(x+\gamma)\right) I_{\frac{N-1}{2}}(\sqrt{x\gamma}) \quad (18)$$

Where,  $\Gamma(x)$  = Gamma function,  $I(x)$  = Bessel function and  $x$ = the sample of the received signal. Therefore the probability of false alarm ( $P_{fa}$ ) is, [4]

$$P_{fa} = Q_{x_N^2}(\lambda) = \int_{\lambda}^{\infty} f_{V'}(x/H_0) dx$$

$$Q_{x_N^2}(\lambda) = \begin{cases} 2Q(\lambda) & \text{if } N = 1 \\ 2Q(\lambda) + \frac{\exp(-\frac{1}{2}\lambda) \sum_{k=1}^{\frac{N-1}{2}} \frac{(k-1)! 2\lambda^{k-\frac{1}{2}}}{(2k-1)!}}{\sqrt{\pi}} & \text{if } N > 1 \text{ and } N \text{ odd} \\ \exp(-\frac{1}{2}\lambda) \sum_{k=0}^{\frac{N-1}{2}} \frac{(\frac{\lambda}{2})^k}{k!} & \text{if } N \text{ is even} \end{cases} \quad (19)$$

By using these equations the threshold  $\lambda$  can be evaluated for specified  $P_{fa}$  and  $N$ .

$$Q(x) = \frac{1}{\sqrt{2\pi}\sigma^2} \int_x^{\infty} \exp\left\{-\frac{x^2}{2\sigma^2}\right\} dx \quad (20)$$

$Q(x)$  is the Gaussian Q function.

For Rayleigh fading channel the threshold is set to meet the specified  $P_{fa}$ . The threshold in a fading channel is to be same as in AWGN channel so for the no transmission of signal  $P_{fa}$  is considered and it is independent of SNR. When signal is present, then the threshold is applied to the data therefore the average probability of detection is computed.

$$P_D = \int_{x_D} P_D(\gamma, \lambda) f_{\gamma}(x) dx \quad (21)$$

Where  $f_{\gamma}(x)$  is the Probability Density Function of the SNR

#### IV. SIMULATION RESULTS

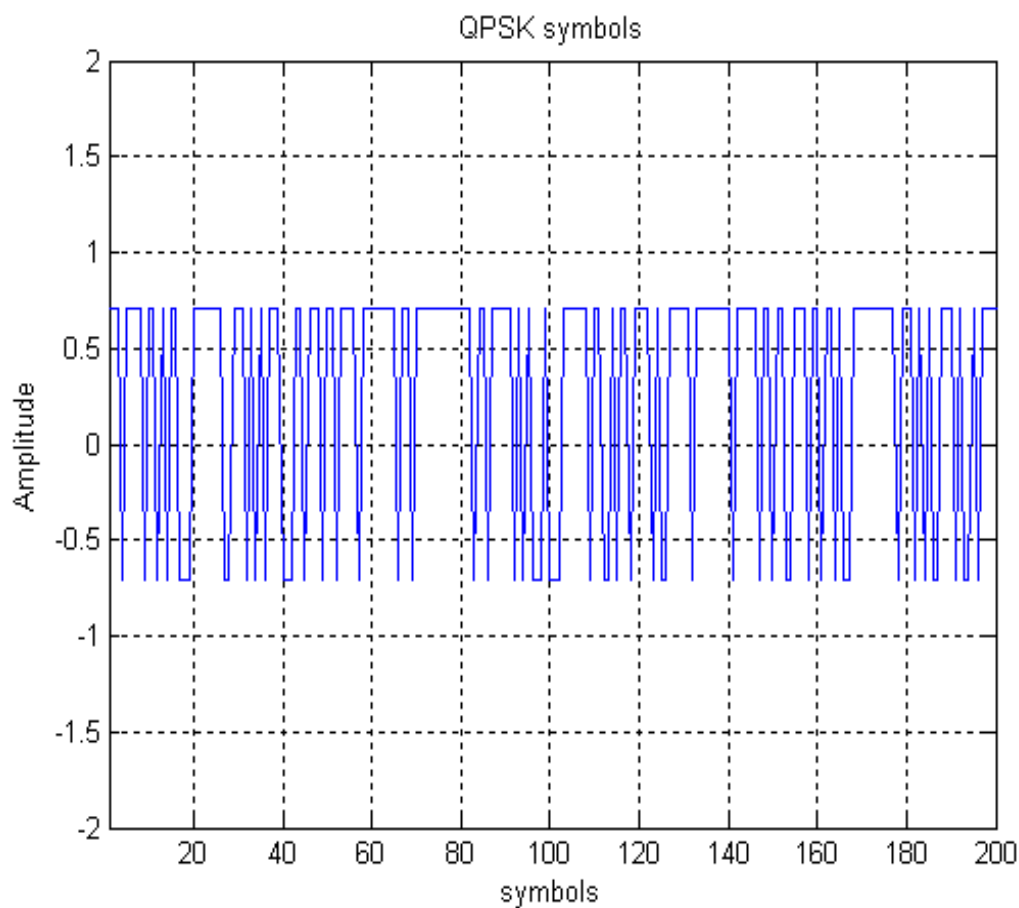


Fig.4 Generation of QPSK Signal

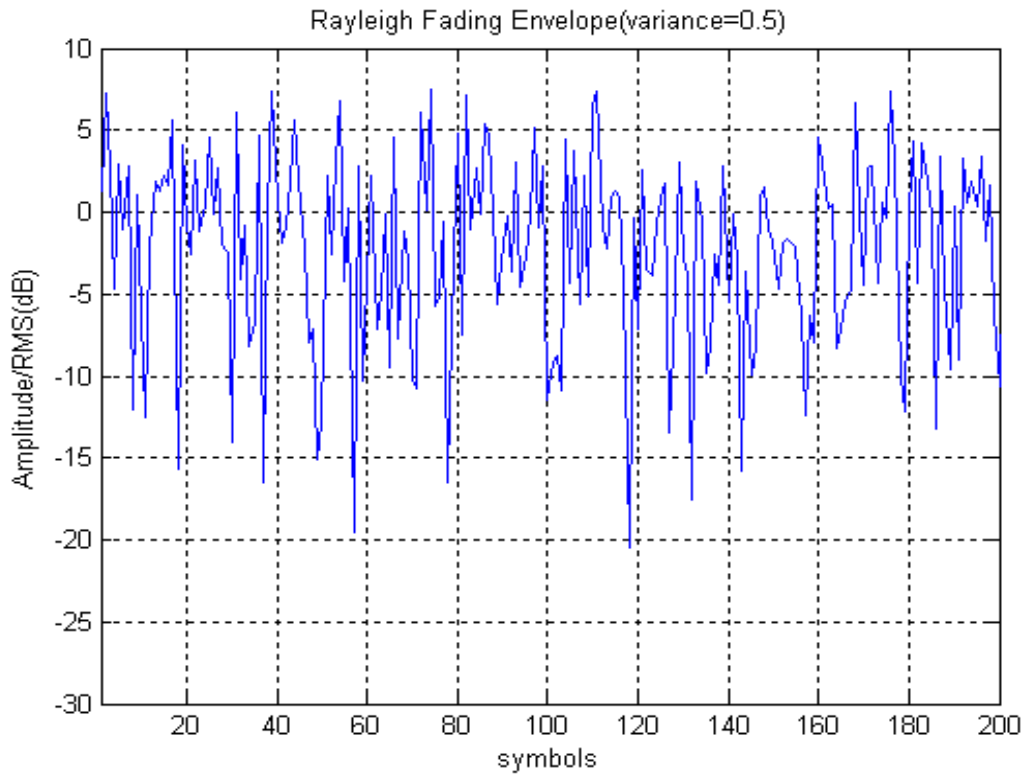


Fig.5 QPSK Signal through Rayleigh Fading

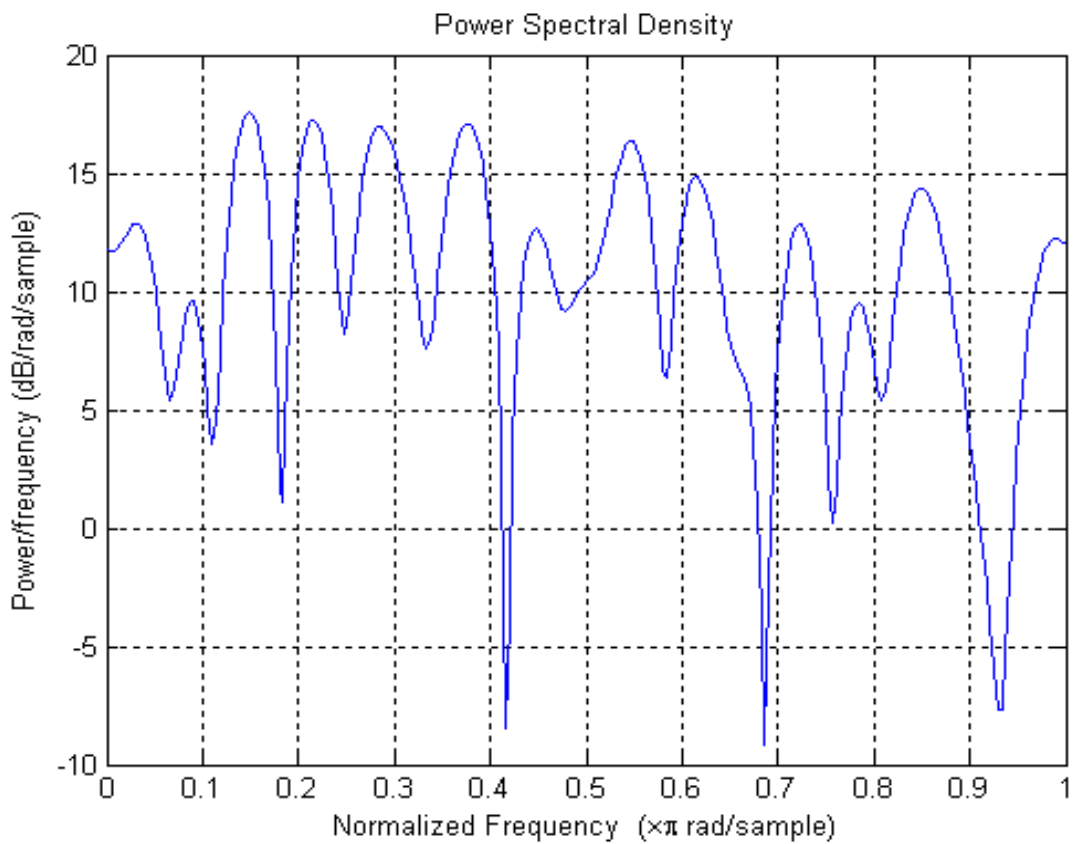


Fig.6 Fading Channel Power Response

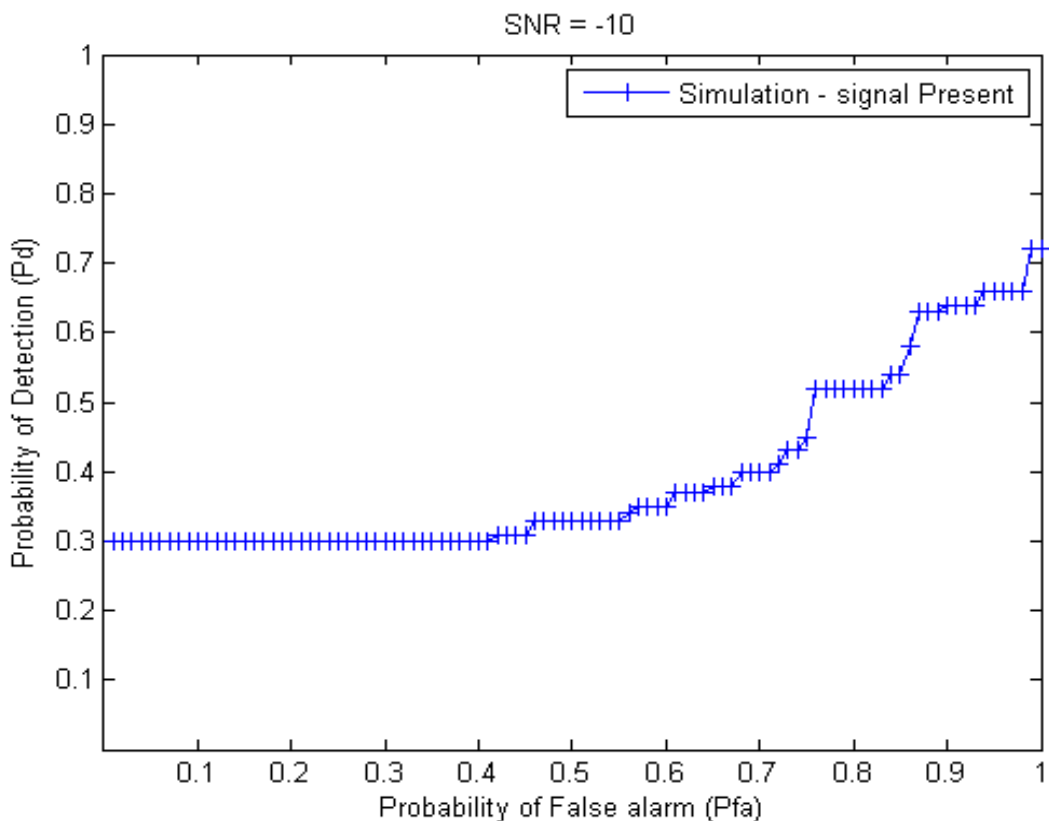


Fig.7 Probability Of Detection ( $P_d$ ) Vs False Alarm ( $P_{fa}$ ) For SNR=-10db

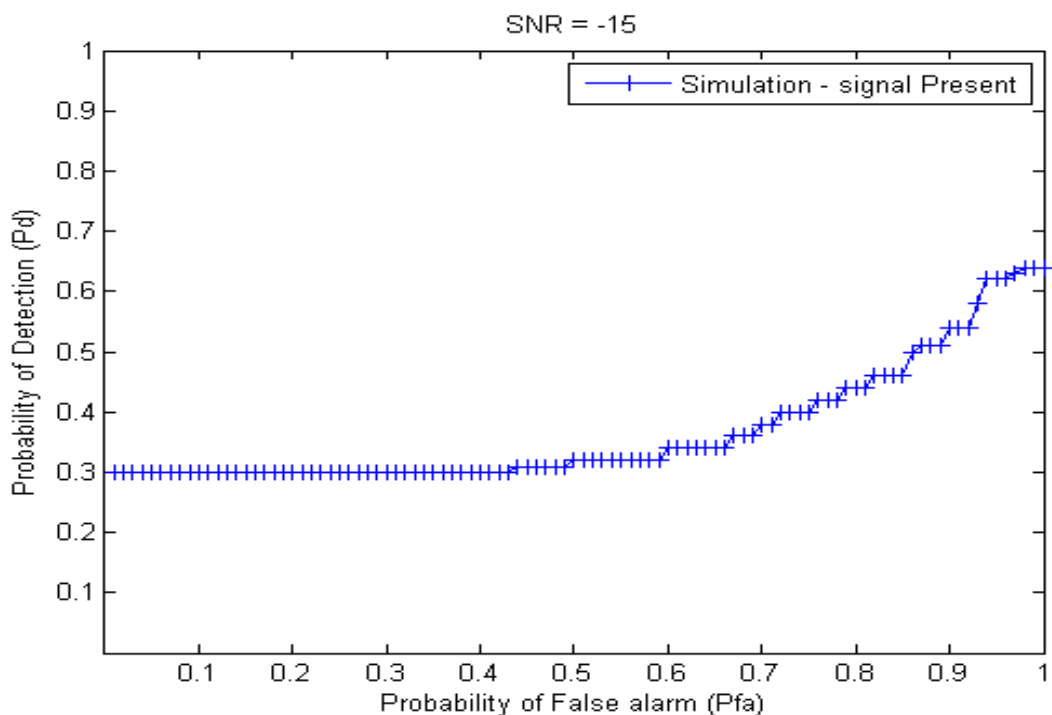
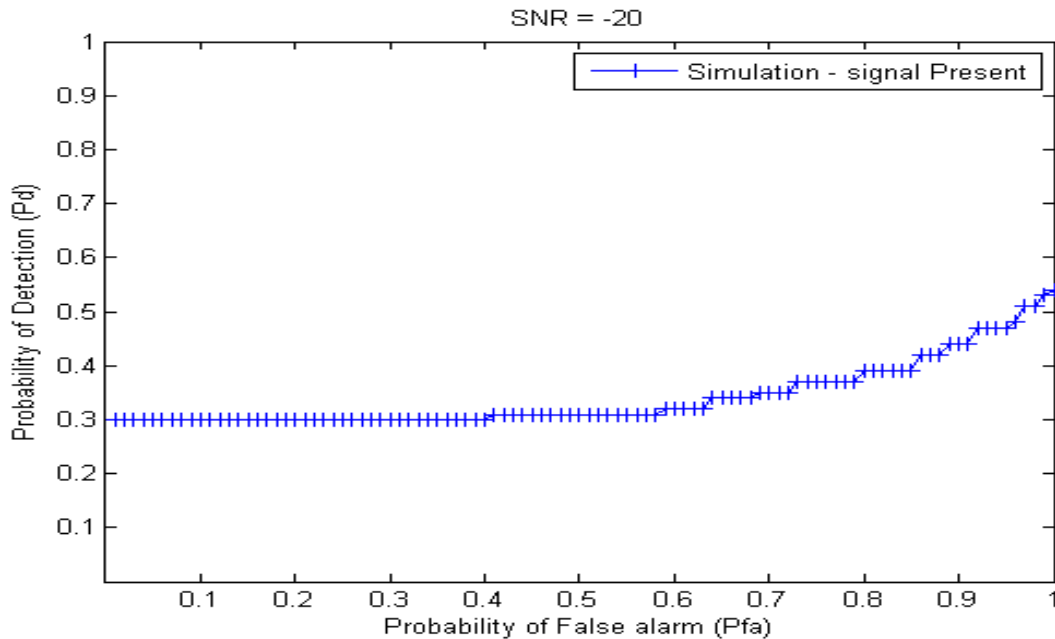


Fig.8 Probability Of Detection ( $P_d$ ) Vs False Alarm( $P_{fa}$ ) For SNR=-15db



**Fig.9 Probability of Detection ( $P_d$ ) Vs False alarm ( $P_{fa}$ ) for SNR=-20db**

### V. CONCLUSION

In this paper we have evaluated the performance of the energy detector in AWGN and Rayleigh fading channels for different SNR. Furthermore the performance is based on the predefined value of  $P_d$  and  $P_{fa}$ . Fig 4 shows the generation of QPSK signals. QPSK modulation type is chosen for the convenience. Fig 5 shows the envelope of QPSK signal through the Rayleigh fading. Fig 6 shows fading channel power response. The performance of the energy detector in fading channel with different SNR is based on measurements. From the Fig 7, 8, 9 shows the performance of  $P_d$  versus  $P_{fa}$  at 20 number of samples for -10db -15db and -20db SNR, it is concluded that the  $P_d$  gradually increases from a lower SNR value of higher SNR values.

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### REFERENCES

- [1] M. McHenry, “Frequency agile spectrum access Technologies in Proc. of FCC Workshop on Cognitive Radio”, May 2003.
- [2] J. P. Wang, L. Xiao, S. Zhou, and J. Wang, “Optimization of detection time for channel efficiency in cognitive radio systems,” ‘IEEE Wireless Commun. And Networking Conf.’ Hong Kong, Mar. 2007, pp.111–115.
- [3] J. B. Anderson and R. Johansson, “Understanding Information Transmission” IEEE press, 2005.
- [4] S.M. Kay, “Fundamentals of Statistical Signal Processing: Detection Theory” Prentice Hall PTR, vol.2,1998.
- [5] WaleedEjaz, NajamulHasan and HyungSeokKim “SNR-Based Adaptive Spectrum Sensing For Cognitive Radio Networks” ‘ICICInternational’ ISSN 1349 4198 Vol.8, pp.6095, September 2012.
- [6] Eeru R. Lavudiya, Dr. K.D. Kulat and Jagdish D. Kene, “Implementation and Analysis of Cognitive Radio System using MATLAB” ‘International Journal of Computer Science and Telecommunications’ Vol.4 Issue 7, July 2013.
- [7] Mahmood A. Abdulsattar and Zahir A. Hussein, “Energy Detection Technique For Spectrum Sensing In Cognitive Radio: A Survey” ‘International Journal of Computer Networks & Communications (IJCNC)’ Vol.4, No.5, September 2012 .
- [8] R. Tandra and A. Sahai “SNR walls for signal detection” ‘IEEE Journal of Selected Topics in Signal Processing’ vol.2, pp.4-17, 2008.